

CLASS 8

MATHS

EXTRA QUESTIONS

Extra Questions for Class 8 Maths Chapter 11: Exploring Some Geometric Themes – HOTS

Original HOTS-level (Higher Order Thinking Skills) practice questions for Class 8 Maths Chapter 11 (Exploring Some Geometric Themes), extending beyond the textbook exercise. Full worked solutions included.

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Q1 (Fractal area at a specific step). For the Sierpinski Gasket (triangle fractal), find the fraction of area remaining after 5 steps, as a decimal rounded to 3 places.

Solution: Area after step $n = (3/4)^n$. After 5 steps: $(3/4)^5 = 243/1024 \approx \mathbf{0.237}$ (about 23.7% of the original area remains).

Q2 (Fractal side count). After how many steps does the Koch Snowflake first have more than 1000 sides?

Solution: Sides at step $n = 3 \times 4^n$. Step 4: $3 \times 256 = 768$ (not enough). Step 5: $3 \times 1024 = 3072$ (exceeds 1000). So **step 5** is the first step with more than 1000 sides.

Q3 (Euler's formula, prism). A prism has 24 edges. If it's a right prism with a regular polygon base, find the number of sides of its base, and its faces and vertices.

Solution: Edges = $3n = 24 \Rightarrow n = \mathbf{8}$ (octagonal base). Faces = $n+2 = \mathbf{10}$. Vertices = $2n = \mathbf{16}$. Check (Euler): $16 - 24 + 10 = 2$. ✓

Q4 (Euler's formula, pyramid). A pyramid has 14 vertices. Find the number of sides of its base, and its faces and edges.

Solution: Vertices = $n+1 = 14 \Rightarrow n = \mathbf{13}$ (13-sided base). Faces = $n+1 = \mathbf{14}$. Edges = $2n = \mathbf{26}$. Check: $14 - 26 + 14 = 2$. ✓

Q5 (Assertion–Reason). Assertion (A): A cube and a square-based pyramid can have the same number of vertices. Reason (R): A cube has 8 vertices, and a square pyramid ($n=4$) has $n+1 = 5$ vertices.

Solution: A cube has 8 vertices; a square pyramid has $4+1 = 5$ vertices — these are **not equal**, so **Assertion is false**. The Reason's arithmetic (5 vertices for a square pyramid) is itself **true**, but since it doesn't match a cube's 8, it does not support the (false) Assertion.

Q6 (Net area, cylinder). A cylinder has radius 7 cm and height 10 cm. Find the area of the rectangular part of its net. (Use $\pi = 22/7$.)

Solution: Rectangle length = circumference = $2\pi r = 2 \times 22/7 \times 7 = 44$ cm. Rectangle area = length $\times$ height = $44 \times 10 = \mathbf{440 \text{ cm}^2}$.

Q7 (Spot the error). A student says: "Since a cube's shadow can be a hexagon, a cube must have 6 identical hexagonal faces." Explain the error.

Solution: Incorrect. A cube always has 6 identical *square* faces — the hexagonal shape only appears as an outline/silhouette when the cube is viewed along a body diagonal (corner-to-corner), because three square faces are then equally visible and their outer edges combine into a hexagon shape. The hexagon is a projection effect, not an actual face of the cube.

Q8 (Combining fractal ideas). If the Sierpinski Carpet starts with a square of area 81 sq. units, find the area remaining after 2 steps.

Solution: Area after step $n = \text{starting area} \times (8/9)^n$. After 2 steps: $81 \times (8/9)^2 = 81 \times 64/81 = \mathbf{64 \text{ sq. units}}$.

Q9 (Net identification, reasoning). A net has 6 squares arranged in a straight row of 4, with one extra square attached above the 2nd square and another attached below the 3rd square. Will this fold into a cube? Explain your reasoning.

Solution: Yes. A row of 4 squares can fold around into 4 of the cube's side faces (like a belt), and the two

extra squares (one above, one below, attached at different points along the row) fold in to become the top and bottom faces — a valid, well-known cube net pattern (this is one of the 11 standard nets, sometimes called the “1-4-1” or cross-like arrangement).

Q10 (Comparing growth rates). Which grows faster as n increases: the number of holes in a Sierpinski Triangle at step n , or the number of sides in a Koch Snowflake at step n ? Explain using the formulas.

Solution: Holes at step $n = (3^n - 1)/2$, which grows like 3^n . Sides at step $n = 3 \times 4^n$, which grows like 4^n . Since 4^n grows faster than 3^n as n increases, **the Koch Snowflake’s side count grows faster** than the Sierpinski Triangle’s hole count.